

Table 2b

Tertiary Tree of Primitive Pythagorean Triples																																																							
Trunk								A ÷ 7	1st Tertiary Branch								A ÷ 7	2nd Tertiary Branches								A ÷ 7	3rd Tertiary Branches								A ÷ 7																				
PPT	r	s	t	A	4A	8A	f		PPT	r	s	t	A	4A	8A	f		PPT	r	s	t	A	4A	8A	f		PPT	r	s	t	A	4A	8A	f																					
<div style="background-color: red; color: white; padding: 5px;"> 3-4-5 2 1 2 6 24 48 1 </div>								<div style="background-color: lightblue; padding: 5px;"> 5-12-13 4 1 8 30 120 240 7 </div>								<h3 style="text-align: center;">Making the “blue”-UPPER & LOWER</h3> <p>$r = \text{even \# satisfying } r^2 = 2st \text{ \& } r^2/2 = st \text{ \& } a = r+s \text{ } b = r+t \text{ } c = r+s+t$</p> <p>for RED 3-4-5 $r=2 \text{ } r^2/2=2^2/2 = 2 = st=1 \cdot 2$; 1,2 become BLUES s values.</p> <p>for RED 3-4-5 Area, $A = (a \cdot b)/2 = (3 \cdot 4)/2 = 6$ and $4A = 4 \cdot 6 = 24$ and the Factor Pairs 4,6 become BLUES r values.</p> <p>Knowing the r & s values for the BLUES, means the rest of the values are also known:</p> <p>if $r = 4$ then $r^2/2 = 4^2/2 = 8$ and since $s=1$, the other Factor Pair, $t = 8$, then $a = r+s = 4+1 = 5 \text{ } b = r+t = 4+8 = 12 \text{ } c = r+s+t = 4+1+8 = 13$ giving the UPPER BLUE 5-12-13 PPT Branch.</p> <p>if $r = 6$ then $r^2/2 = 6^2/2 = 18$ and since $s = 2$, the other Factor Pair, $t = 9$, then $a = r+s = 6+2 = 8 \text{ } b = r+t = 6+9 = 15 \text{ } c = r+s+t = 6+2+8 = 17$ giving the LOWER BLUE 8-15-17 PPT Branch.</p> <p>They both have the same f-value as $f = b - a$:</p> <p>for 5-12-13 $b-a = 12 - 5 = 7$ for 8-15-17 $b-a = 15 - 8 = 7$ (The f-value also = the Σ of RED 3+4=7)</p> <p>Hint: The MEDIUM Branch is a hybrid of the RED & BLUE- see Table 2c</p>								<div style="background-color: lightblue; padding: 5px;"> 20-21-29 12 8 9 210 840 1680 1 ✓ </div>								<div style="background-color: lightblue; padding: 5px;"> 8-15-17 6 2 9 60 240 480 7 </div>																							
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<p>Key: PPT=Primitive Pythagorean Triple; r=even # such that $r^2/2=st$ where s,t are Factor Pairs; A=Area; 4A=4Area; 8A=8Area; $f=b-a$ & $f^2=(b-a)^2$, as $a^2 + b^2 = c^2 = 4A + f^2 = (8A + f^2) - 4A$</p> <p>The Tree of Pythagorean Triples branches from the 3-4-5 PPT trunk first into a 3-part main branch, each of which further branches into 2nd, 3rd, 4th, ..., tertiary branches. Each tertiary follows the lead f-value of its predecessor, but is actually formed as an intermediary to the upper and lower branches of which it is a part. All PPTs — with no repeats — are to be found. Pythagoras first discovered the UPPER branch sequence, Plato (a century later) discovered the LOWER branch sequence. The MIDDLE branch sequence follows as an intermediary, hybrid sequence of the UPPER and LOWER.</p> <p>Using the <i>Expanded Dickson Method</i> on the BBS-ISL Matrix, every PPT branch is accounted for by the previous branch. This is done by enlisting the r,s,t,A,4A,8A,f associated values. All these values are derived directly from the respective PTT by both algebra and geometry. In Table 2a we looked at the overall. In Table 2b, we examine how the UPPER and LOWER branches (blue) are made from the trunk (red). In Table 2c, we see how the MIDDLE branch (red) is formed from the UPPER and LOWER (blue) branches and the trunk (red). As a <u>fractal</u>, this Number Pattern Sequence that defines the first branchings, continues through the entire tree. Table 2d shows BLUE branching to 2nd Tertiary Branches. Table 2e reveals the power of f. Table 2f tells all.</p> <p>Copyright © 2017, Reginald Brooks</p>																																																							